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# Slant Correction in an Optimization Framework

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# In this presentation ...

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## Topic 1

**Non-uniform slant correction  
for handwritten word**

and

## Topic 2 (planning phase)

**Non-uniform skew correction  
for scanned document**

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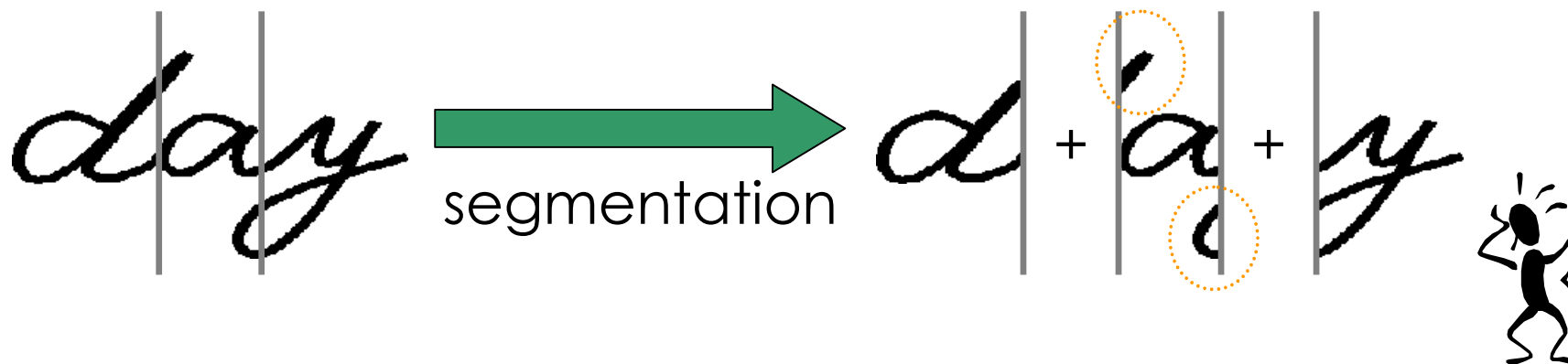
# *Topic 1*

## **Non-uniform slant correction for handwritten word**

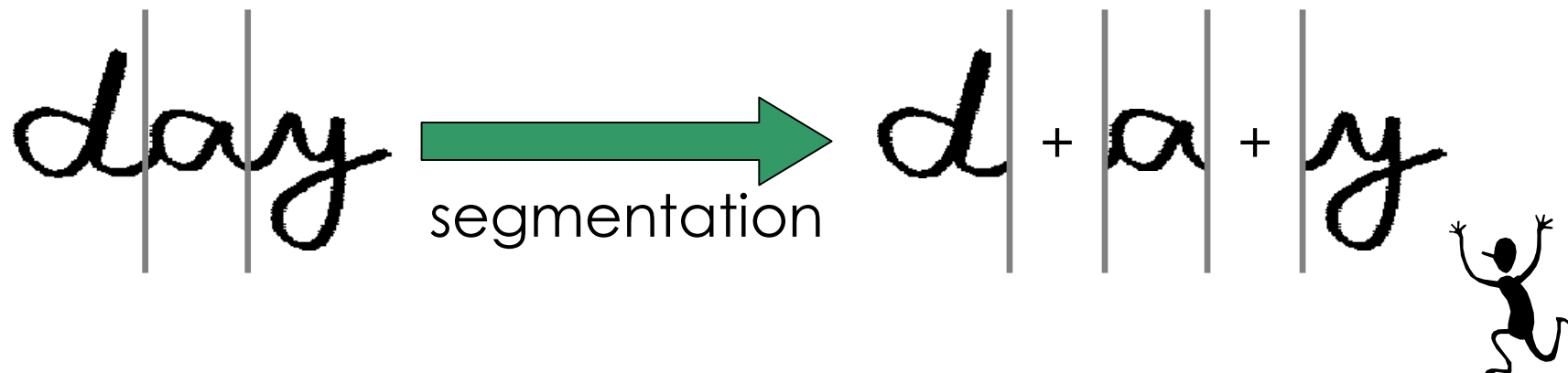
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# Slant correction of handwritten word

## Handwritten word

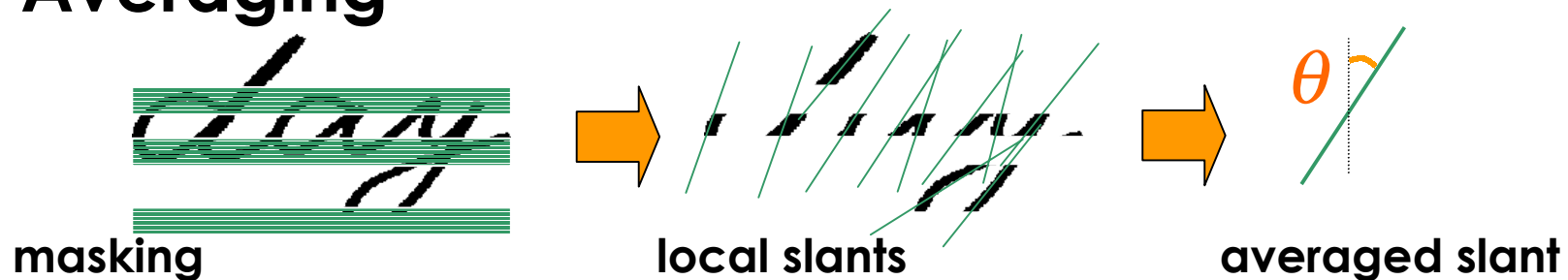


## Slant-corrected word



# Conventional techniques

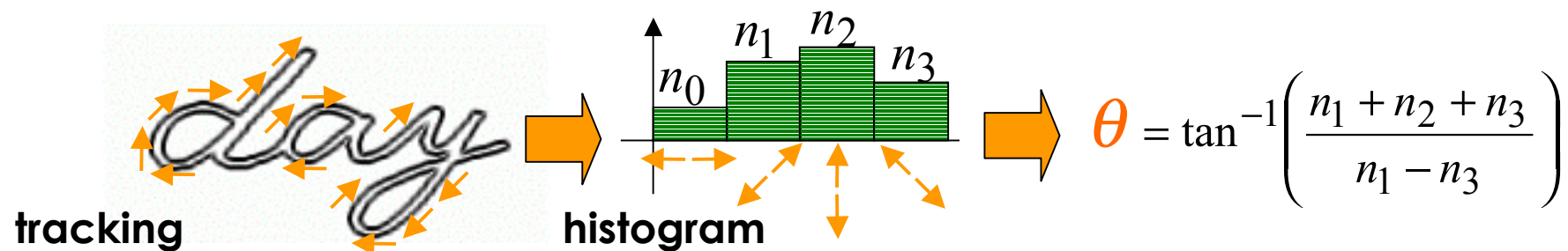
## ■ Averaging



## ■ Projection histograms

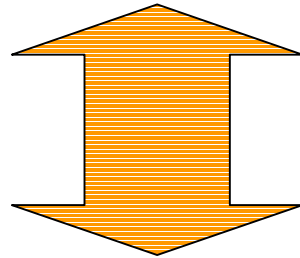


## ■ Statistics of chain-coded stroke contours

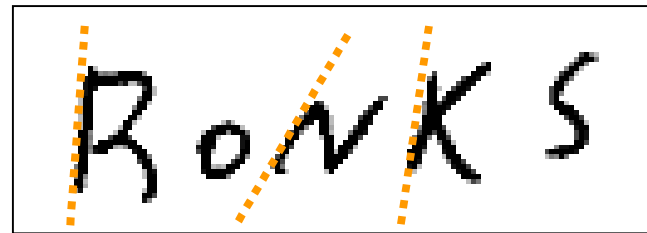
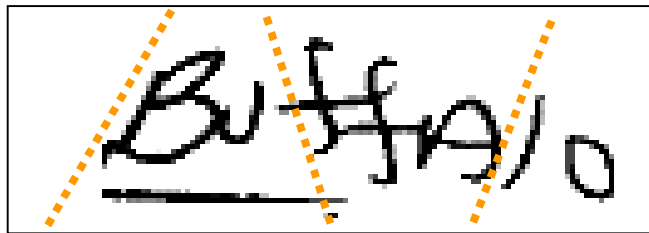


# Conventional techniques : the problem

Assumption in all conventional techniques :  
*Slant is uniform in a word*

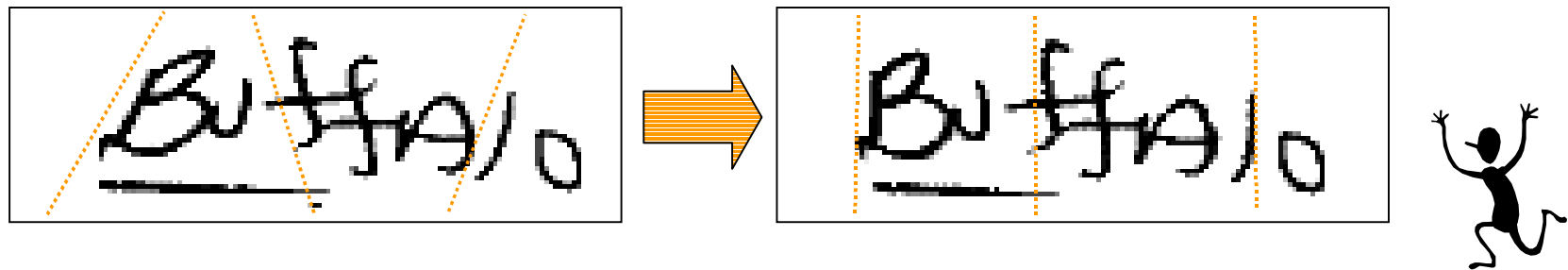


But.... sometimes, slant is **non-uniform**  
(with a probability of 5 to 10%)



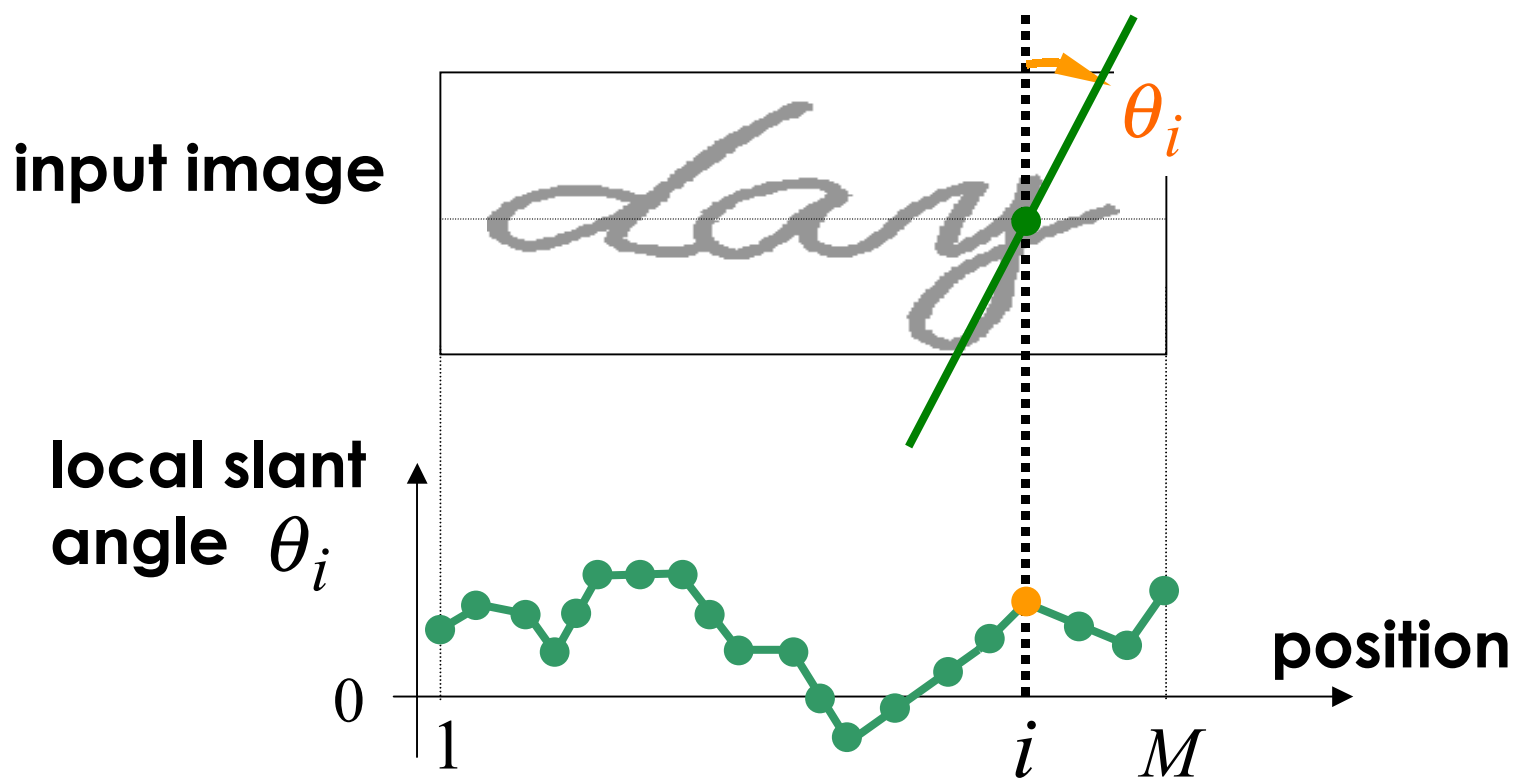
# Overview of the present technique

- Estimation and correction of **non-uniform slant** in an optimization framework



- Simple and fast algorithm based on **dynamic programming (DP)**

# Non-uniform slant correction as an optimal estimation problem

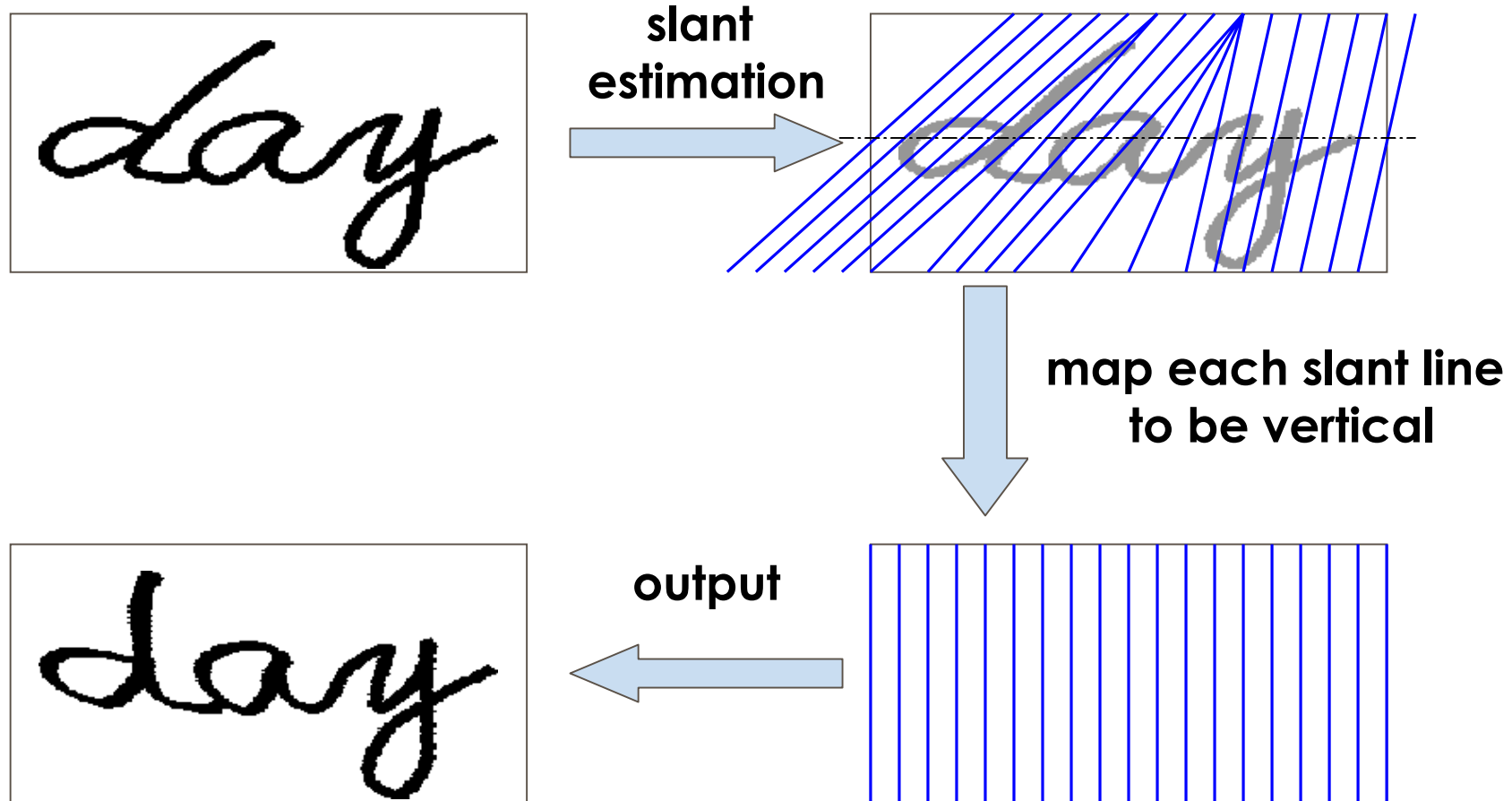


non-uniform slant correction

= optimal estimation of  $\theta_1, \dots, \theta_i, \dots, \theta_M$



# Create slant-corrected image using estimated slant



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# Directions on designing the criterion for the optimal estimation

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Detect long vertical strokes

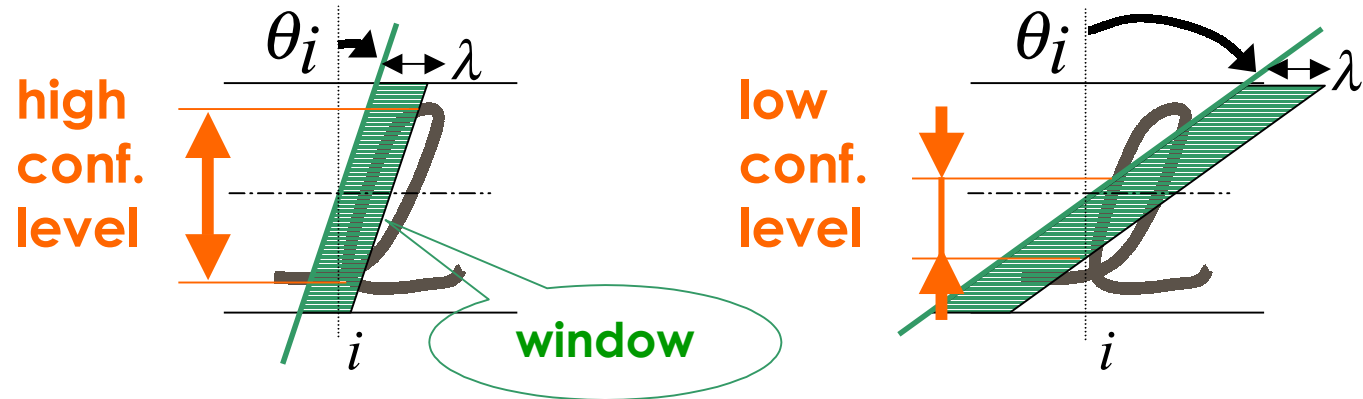
and

Propagate their slant angles  
to their neighborhood smoothly

# Our criterion

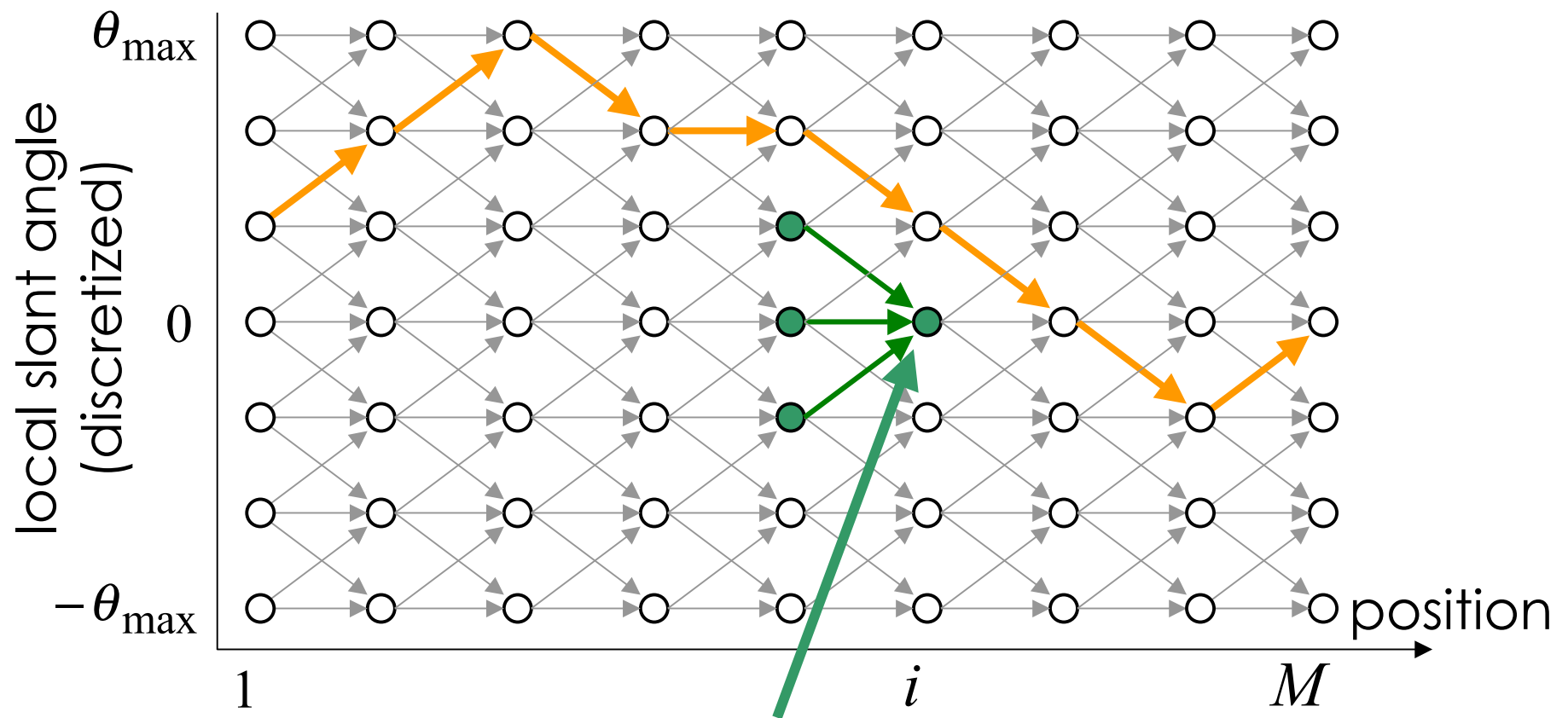
$$\text{maximize } \sum_{i=1}^M [s_i(\theta_i) + \rho(\theta_i | \theta_{i-1})]$$

■  $s_i(\theta_i)$  : confidence level of  $\theta_i$  at position  $i$



■  $\rho(\theta_i | \theta_{i-1})$  : continuity between  $\theta_i$  and  $\theta_{i-1}$

# Algorithm based on dynamic programming



DP recursion

$$g_i(\theta_i) = s_i(\theta_i) + \max_{\theta_{i-1}} [g_{i-1}(\theta_{i-1}) + \rho(\theta_i | \theta_{i-1})]$$

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# Computational complexity

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- Theoretical :

$$O(MNW)$$

where  $M$ =width,  $N$ =height, and  $W$ =max slant

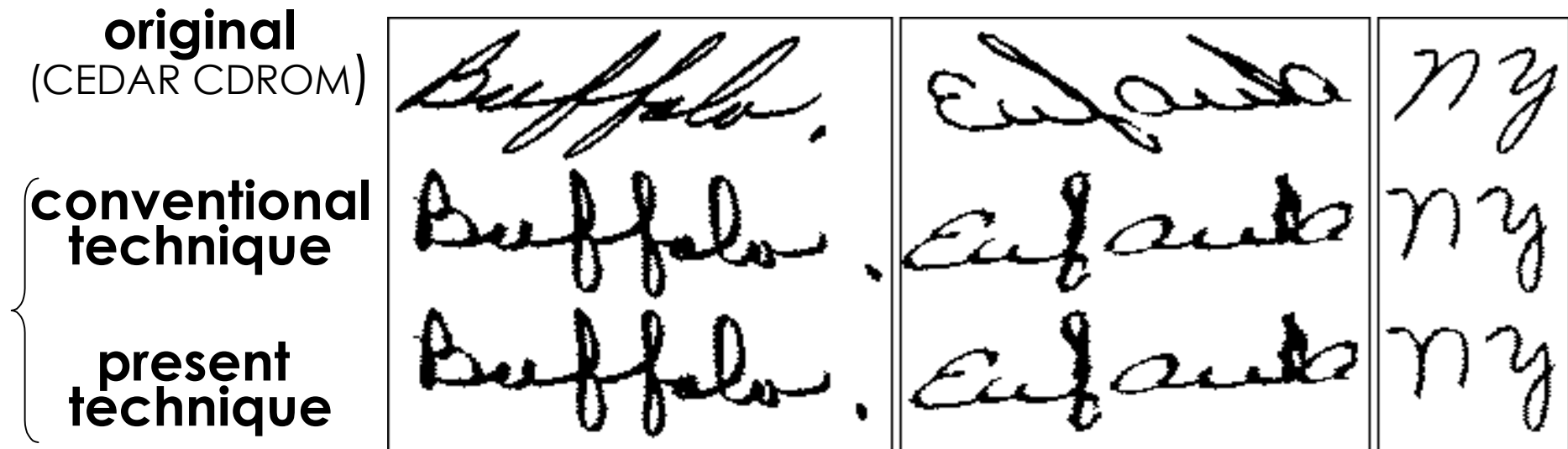
- Practical :

**140 ms** (latest result)

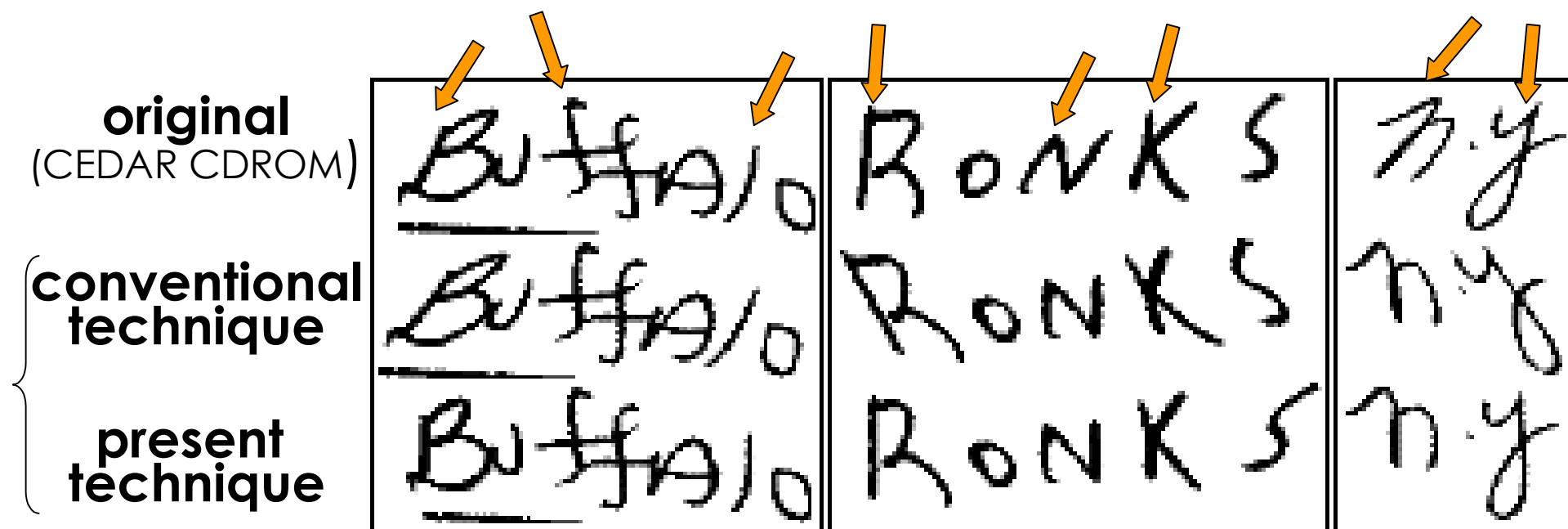
for  $M=256$ ,  $N=64$ , and  $W=60$ (degrees)  
at PC with Pentium III, 500MHz

# Results (1) :

## Correction of near uniform slant



# Results (2) : Correction of non-uniform slant



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# Quantitative evaluation (1)

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- **Mean estimation error** was measured using artificially slanted words

- Two slant patterns were used



The image shows the word "Kentucky" written in a cursive font. The slant of the letters is constant throughout the word, meaning the angle of the pen strokes does not change.

constant



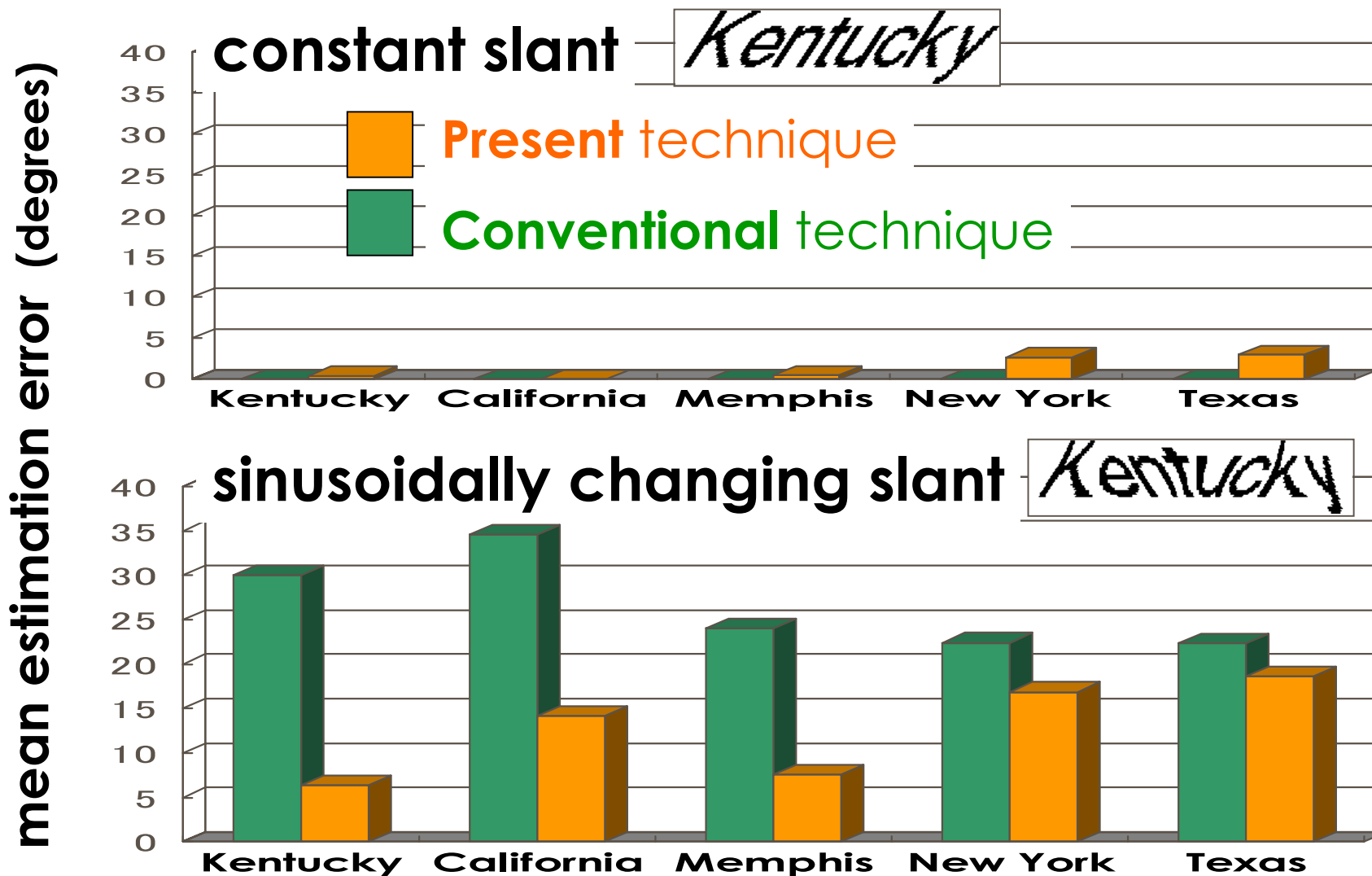
The image shows the word "Kentucky" written in a cursive font. The slant of the letters varies sinusoidally, meaning the angle of the pen strokes oscillates in a wave-like pattern across the word.

sinusoidal

- **5 city name words were subjected**  
(Kentucky, California, Memphis, New York, Texas)

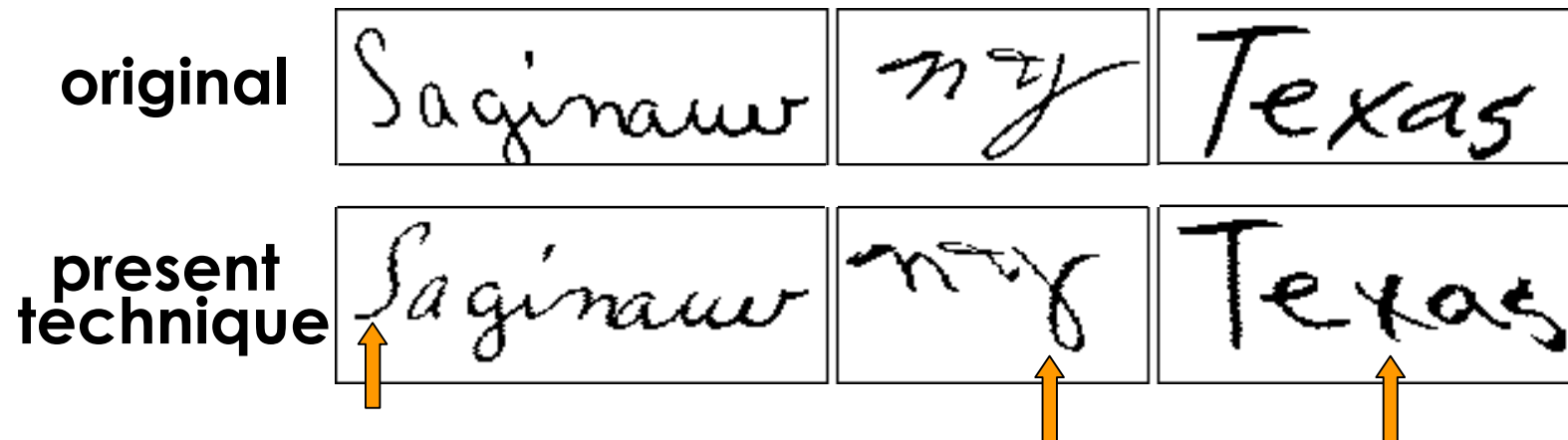


# Quantitative evaluation (2)



# Remaining problem: over-correction

## ■ Examples



## ■ Cause : originally slanted parts



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# Conclusion of first part

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- **Formulate the non-uniform slant correction problem as an optimization problem**
- **Provide a simple and fast algorithm based on dynamic programming**
- **Indicate superiority over conventional techniques through experiments**

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## *Topic 2 (planning phase)*

# **Non-uniform skew correction for scanned document**

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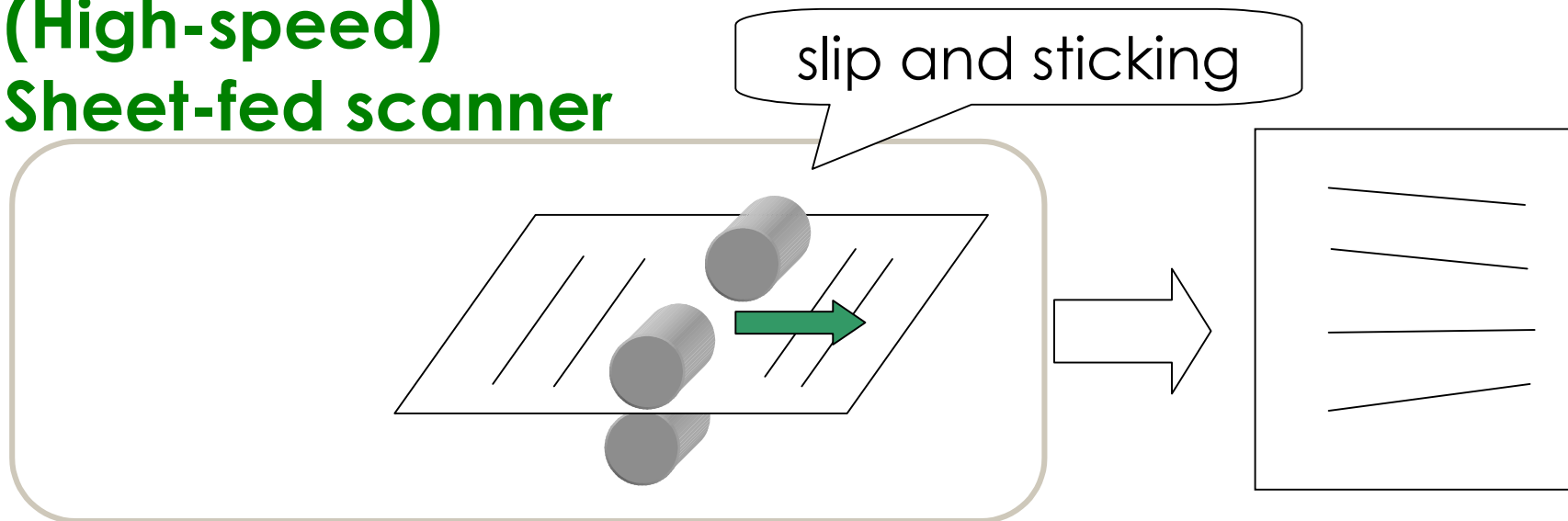
# Purpose and methodology

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- **Remove non-uniform skew** in scanned document
- Use an algorithm similar to the foregoing non-uniform slant correction algorithm

# Types of non-uniform skew (1): Skew due to paper feeding

(High-speed)  
Sheet-fed scanner

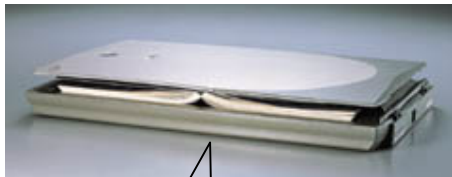


cf. Hirano-Okada-Yoda (2001, ICDAR)

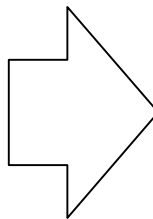
non-uniform skew correction by affine transformation

# Types of non-uniform skew (2): Skew due to the thickness of book

## Flatbed scanner



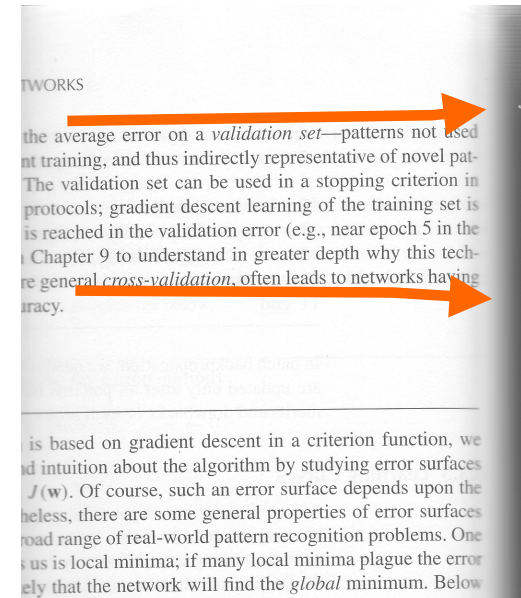
book



o occlusion, and even minor misspecifications of the model. Grammatical methods have been abandoned for object recognition [60, 25]. Grammatical methods have been applied to the example, highly structured diagrams, such as electrical circuit diagrams, Chinese/Japanese kanji characters. For useful surveys of the state of the art in pattern recognition see references [13, 14, 32, 33, 34] and [28], and for grammatical inference see references [3] and [28], and for grammatical inference see references [3] and [28]. The complexity of parsing type 3 grammars is linear in the length of the string; type 2 is low-order polynomial, type 1 is exponential; pointers to relevant papers appear in [76]. There has been a great deal of work on parsing natural language, and a good textbook on artificial intelligence addressing this area is reference [75]. There is much work on inferring grammars from data, such as the Crespi-Reghizzi algorithm (context free) [22]. In the context of interactive learning, the learning of a grammar can be accelerated [81].

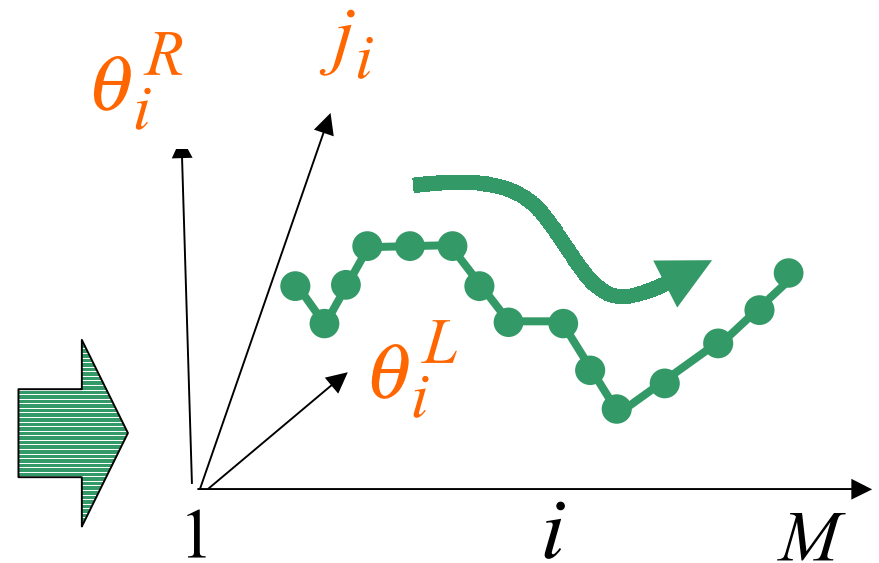
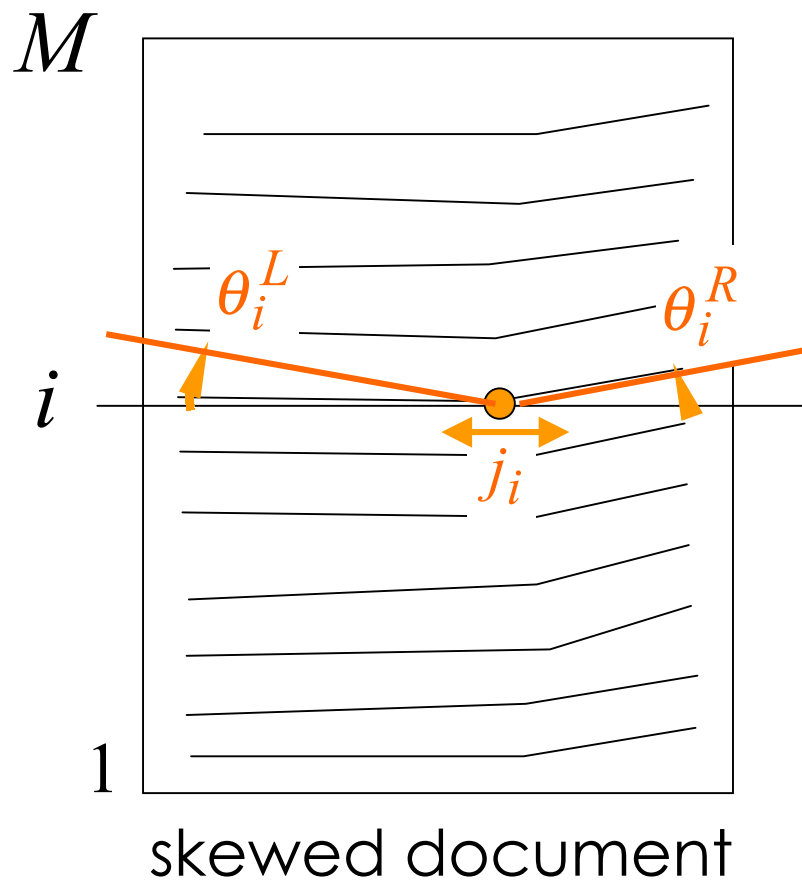
ed in this chapter have been expanded to allow for stochastic grammars. There are probabilities associated with rules [20]. A grammar is a specification of a prior probability for a class—for instance, for legal strings in the language  $\mathcal{L}$ . Error-correcting parsers are used to handle random variations arise in an underlying stochastic grammar. They apply probability measures to languages [8].

have formed the foundation of expert systems, and they have been used in many branches of artificial intelligence such as natural language prediction; their use in pattern recognition has been demonstrated in several systems include DENDRAL, for inferring chemical structures [29], PROSPECTOR, for finding mineral deposits [30], and PROSPECTOR for medical diagnosis [79]. Early use of rule induction for pattern recognition is due to Michalski [57, 58]. Figure 8.17 was inspired by Wilson's work on learning simple geometrical structures and relationships [57]. It can be called inductive logic programming; Clark and Niblett [57].



## Curvilinear distortion

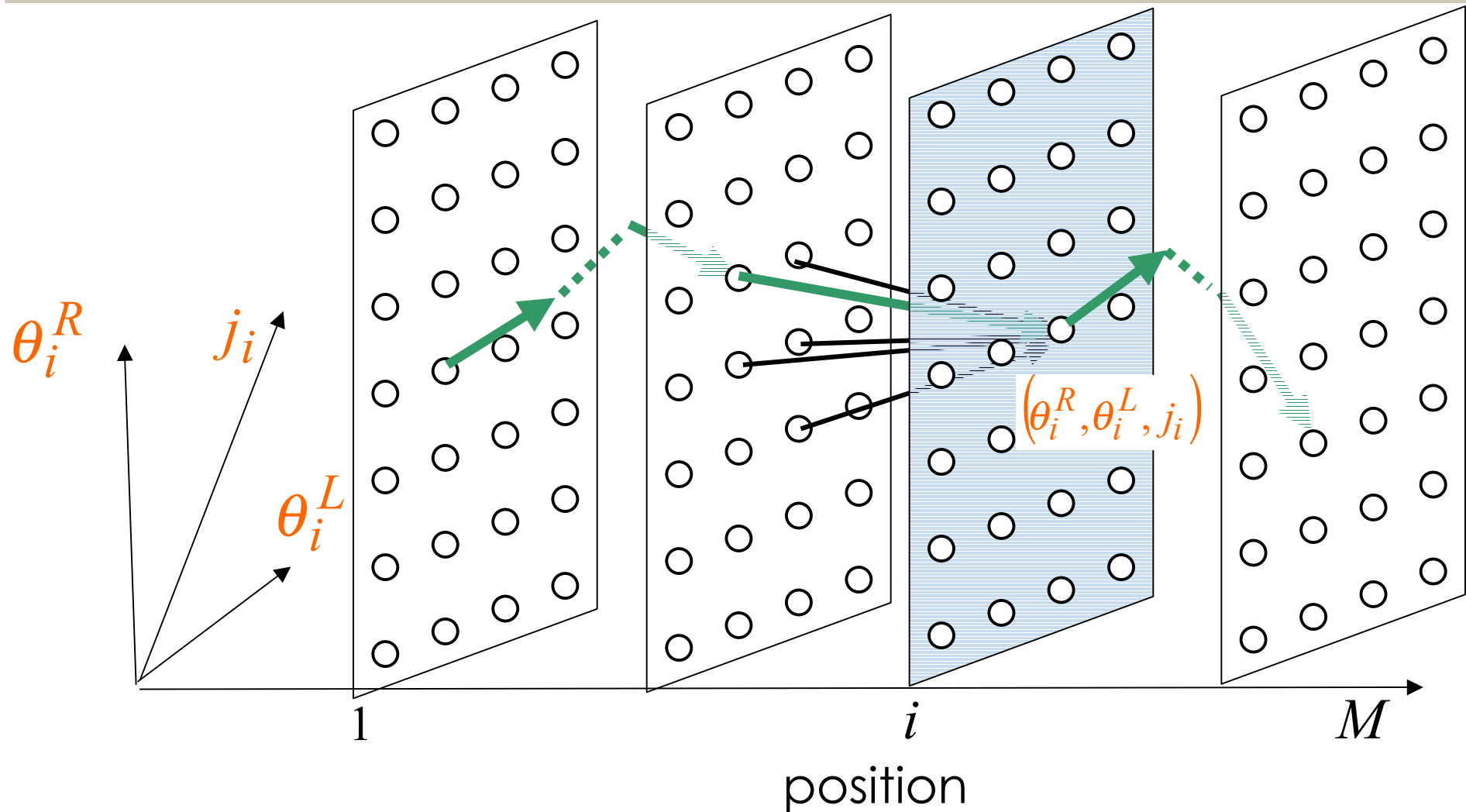
# Model of non-uniform skew



non-uniform skew  
represented as the  
sequence of  $(\theta_i^R, \theta_i^L, j_i)$



# Algorithm based on dynamic programming



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# Future work for non-uniform skew correction

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- **Collect skewed documents  
and observe their characteristics**
- **Design criterion**
- **Evaluate the technique**